# 61A Lecture 17

Wednesday, March 4

#### Announcements

• Delayed: Hog contest winners will be announced Friday 3/6 in lecture

• Quiz 2 due Thursday 3/5 @ 11:59pm (challenging!)

• Project 3 due Thursday 3/12 @ 11:59pm (get started now!)

• Delayed: Homework 6 due Monday 3/16 @ 11:59pm

•Midterm 2 is on Thursday 3/19 7pm-9pm

Emphasis: mutable data, object-oriented programming, recursion, and recursive data

**Generic Functions of Multiple Arguments** 

# **More Generic Functions**

A function might want to operate on multiple data types

#### Last lecture:

- Polymorphic functions using shared messages
- Interfaces: collections of messages that have specific behavior conditions
- Two interchangeable implementations of complex numbers

#### This lecture:

- An arithmetic system over related types
- Operator overloading
- •Type dispatching
- •Type coercion

#### **Rational Numbers**



**Complex Numbers** 

```
class Complex:
                       def add(self, other):
                            return ComplexRI(self.real + other.real,
                                               self.imag + other.imag)
                       def mul(self, other):
                            return ComplexMA(self.magnitude * other.magnitude,
                                               self.angle + other.angle)
                                                         class ComplexMA(Complex):
class ComplexRI(Complex):
                                                             """A polar representation."""
   """A rectangular representation."""
   def init (self, real, imag):
                                                             def __init__(self, magnitude, angle):
       self.real = real
                                                                 self.magnitude = magnitude
       self.imag = imag
                                                                 self.angle = angle
   @property
                                                             @property
   def magnitude(self):
                                                             def real(self):
       return (self.real ** 2 + self.imag ** 2) ** 0.5
                                                                 return self.magnitude * cos(self.angle)
   @property
                                                             @property
                                                             def imag(self):
   def angle(self):
       return atan2(self.imag, self.real)
                                                                 return self.magnitude * sin(self.angle)
                                                 (Demo)
```

### Cross-Type Arithmetic Examples

Currently, we can add rationals to rationals, but not rationals to complex numbers

	<pre>&gt;&gt;&gt; Rational(3, 14).add(Rational(2, 7))</pre>	$\frac{3}{14} + \frac{2}{7}$
Shared	Rational(1, 2)	14 7
interface	<pre>&gt;&gt;&gt; ComplexRI(0, 1).mul(ComplexMA(1, 0.5 * pi))</pre>	$i\cdot i$
	ComplexMA(1, 1 * pi)	
	<pre>&gt;&gt;&gt; Rational(3, 14) + Rational(2, 7)</pre>	$\frac{3}{1} + \frac{2}{7}$
	Rational(1, 2)	14 7
Operators	<pre>&gt;&gt;&gt; ComplexRI(0, 1) * ComplexMA(1, 0.5 * pi)</pre>	$i\cdot i$
	ComplexMA(1, 1 * pi)	
Cross-type	<pre>&gt;&gt;&gt; Rational(1, 2) + ComplexRI(0.5, 2)</pre>	$\frac{1}{1} + (0.5 + 2 \cdot i)$
	ComplexRI(1, 2)	2
arithmetic	<pre>&gt;&gt;&gt; ComplexMA(2, 0.5 * pi) * Rational(3, 2)</pre>	$2 \cdot i \cdot \frac{3}{-}$
	ComplexMA(3, 0.5 * pi)	2

**Special Method Names** 

#### Special Method Names in Python

Certain names are special because they have built-in behavior

These names always start and end with two underscores

init	Method invoked automatically when an object is constructed
repr	Method invoked to display an object as a string
add	Method invoked to add one object to another
bool	Method invoked to convert an object to True or False

```
>>> zero, one, two = 0, 1, 2
>>> one + two
3
>>> bool(zero), bool(one)
(False, True)

Same
behavior
using
methods
>>> zero._bool_(), one._bool_()
(False, True)
```

9

### **Special Methods**

```
Adding instances of user-defined classes invokes the __add__ method
    class Number:
                                                class Rational(Number):
        """A number."""
                                                    def add(self, other):
        def __add__(self, other):
            return self.add(other)
                                                    def mul(self, other):
                                                        . . .
        def mul (self, other):
            return self.mul(other)
                                                class Complex(Number):
                                                    def add(self, other):
    >>> Rational(1, 3) + Rational(1, 6)
                                                    def mul(self, other):
    Rational(1, 2)
                                                        . . .
```

We can also <u>\_\_add\_\_</u> complex numbers, even with multiple representations (Demo)

http://getpython3.com/diveintopython3/special-method-names.html

http://docs.python.org/py3k/reference/datamodel.html#special-method-names

Type Dispatching

The Independence of Data Types

Data abstraction and class definitions keep types separate

Some operations need access to the implementation of two different abstractions

How do we add a complex number and a rational number together?

Rational numbers as numerators & denominators

&

Complex numbers as two-dimensional vectors

def add\_complex\_and\_rational(c, r):
 """Return c + r for complex c and rational r."""
 return ComplexRI(c.real + r.numer/r.denom, c.imag)

### Type Dispatching

Define a different function for each possible combination of types for which an operation (e.g., addition) is valid



Type Dispatching Analysis

### Type Dispatching Analysis

Minimal violation of abstraction barriers: we define cross-type functions as necessary

Extensible: Any new numeric type can "install" itself into the existing system by adding new entries to the cross-type function dictionaries

Number.adders[(tag0, tag1)] = add\_tag0\_and\_tag1

Question: How many cross-type implementations are required for *m* types and *n* operations?

15

# Type Dispatching Analysis

Minimal violation of abstraction barriers: we define cross-type functions as necessary.

Extensible: Any new numeric type can "install" itself into the existing system by adding new entries to the cross-type function dictionaries

Arg 1	Arg 2	Add	Multiply
Complex	Complex		
Rational	Rational		
Complex	Rational		
Rational	Complex		

**Type Coercion** 

### Coercion

Idea: Some types can be converted into other types

Takes advantage of structure in the type system

```
def rational_to_complex(r):
    """Return complex equal to rational."""
    return ComplexRI(r.numer/r.denom, 0)
```

Question: Can any numeric type be coerced into any other?

Question: Can any two numeric types be coerced into a common type?

```
Question: Is coercion exact?
```

# Applying Operators with Coercion



#### **Coercion Analysis**

Minimal violation of abstraction barriers: we define cross-type coercion as necessary Requires that all types can be coerced into a common type More sharing: All operators use the same coercion scheme

Arg 1	Arg 2	Arg 2		Add		Multiply	
Complex	Comple	Complex					
Rational	Rationa	Rational					
Complex	Rationa	Rational					
Rational	Comple	ex					
				$\sum$			
From	То	Coerce		Туре	Add	Multiply	
Complex	Rational			Complex			
Rational	Complex			Rational			