

61A Lecture 33

Monday, April 20

Announcements

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- Course survey due Monday 4/20 @ 11:59pm

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- If 85% of students complete the course survey on resources, everyone gets 1 bonus point!

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<http://goo.gl/ajEBkT>

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- Project 4 due Thursday 4/23 @ 11:59pm

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- Project 4 due Thursday 4/23 @ 11:59pm
 - Early point #2: All questions (including Extra Credit) by Wednesday 4/22 @ 11:59pm

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- Recursive Art Contest Entries due Monday 4/27 @ 11:59pm

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- Recursive Art Contest Entries due Monday 4/27 @ 11:59pm
 - Email your code & a screenshot of your art to cs61a-tae@imail.eecs.berkeley.edu (Albert)

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- Project 4 due Thursday 4/23 @ 11:59pm
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- Recursive Art Contest Entries due Monday 4/27 @ 11:59pm
 - Email your code & a screenshot of your art to cs61a-tae@imail.eecs.berkeley.edu (Albert)
- Homework 9 merged with Homework 10; both are due Wednesday 4/29 @ 11:59pm

Local Tables

Local Tables

A `create table` statement names a table globally

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```
create table parents as
  select "abraham" as parent, "barack" as child union
  select "abraham"      , "clinton"      union
  select "delano"       , "herbert"     union
  select "fillmore"    , "abraham"   union
  select "fillmore"    , "delano"    union
  select "fillmore"    , "grover"    union
  select "eisenhower"  , "fillmore";
```

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  select "abraham"      , "clinton"      union
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  select "fillmore"    , "abraham"   union
  select "fillmore"    , "delano"    union
  select "fillmore"    , "grover"    union
  select "eisenhower" , "fillmore";
```

parents:

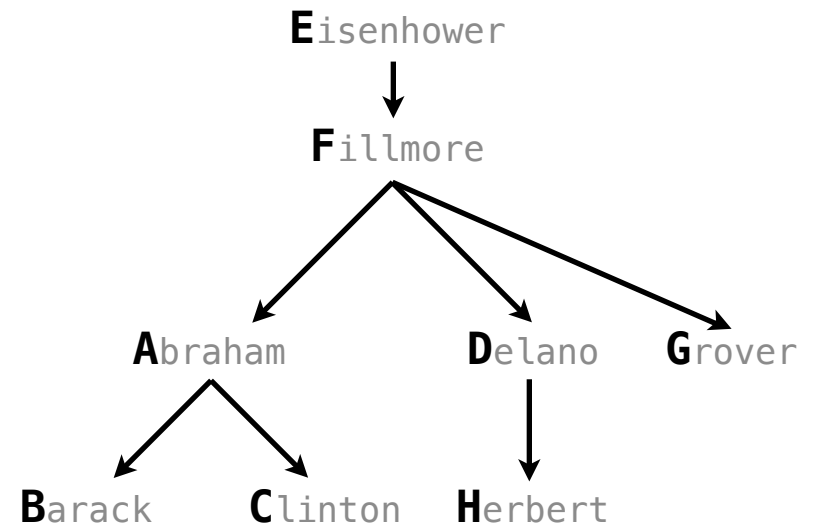
Parent	Child
abraham	barack
abraham	clinton
delano	herbert
fillmore	abraham
fillmore	delano
fillmore	grover
eisenhower	fillmore

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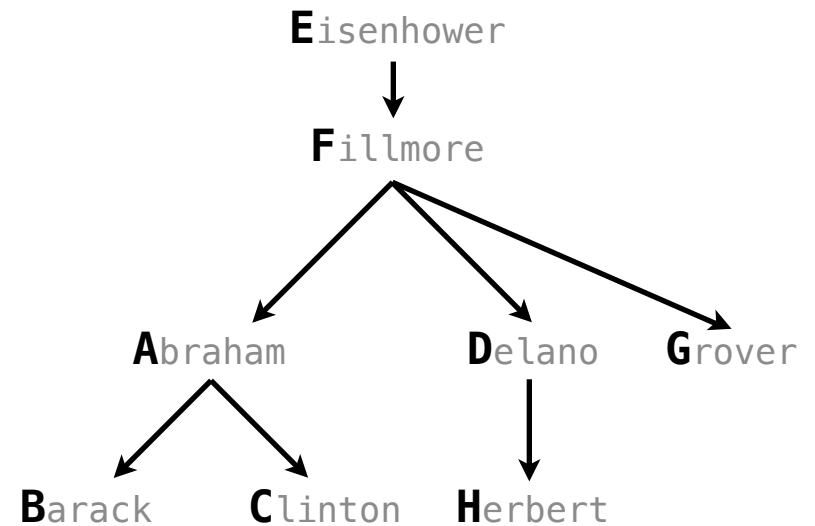
Local Tables

A `create table` statement names a table globally

A `with` clause of a `select` statement names a table that is local to the statement

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create table parents as
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  ...
```

parents:

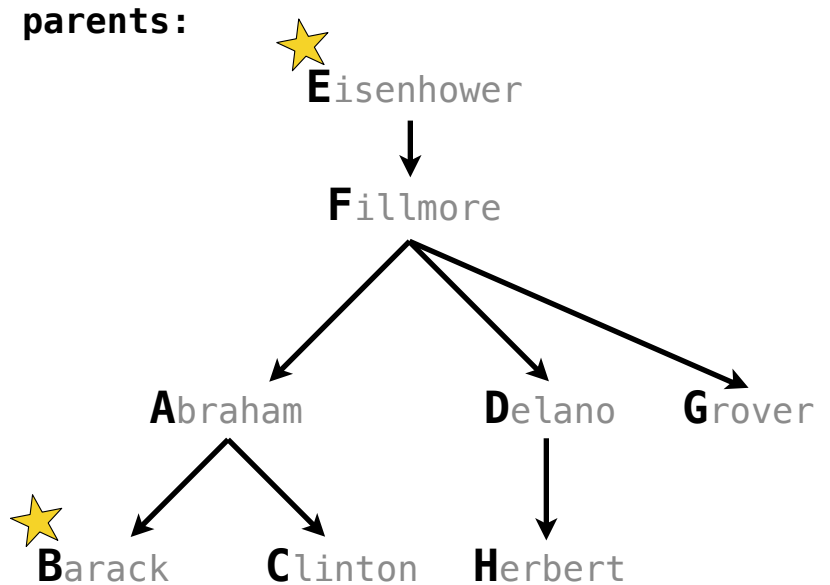


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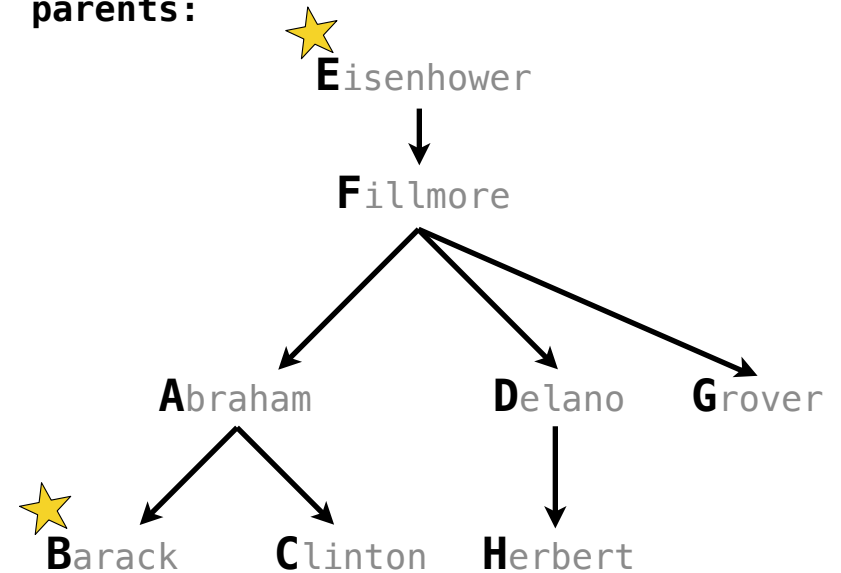
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```

```
select parent from ...
```

parents:



Local Tables

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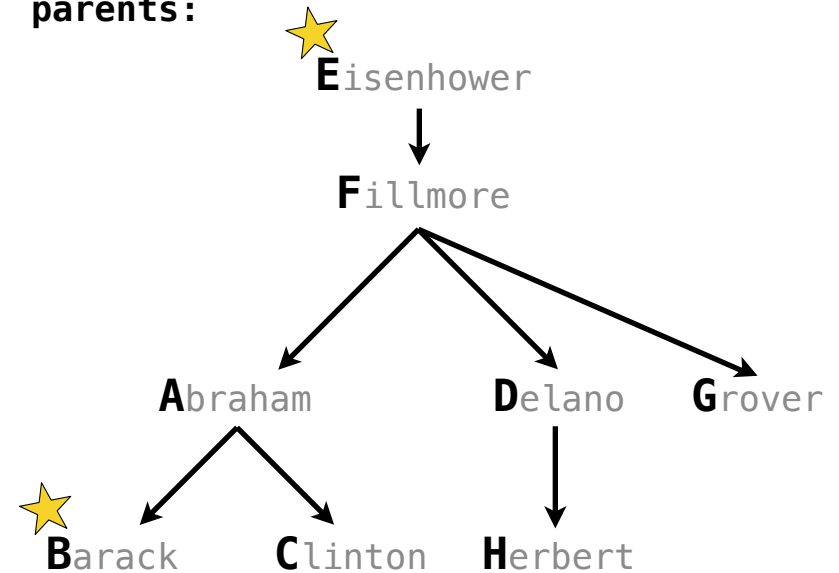
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parents:



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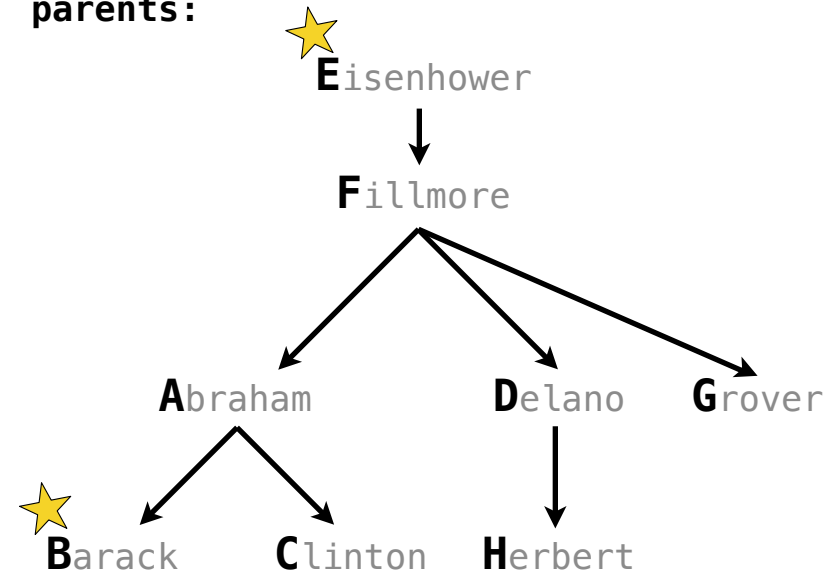
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create table parents as
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with

```
best(dog) as (
```

```
select parent from ...
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parents:



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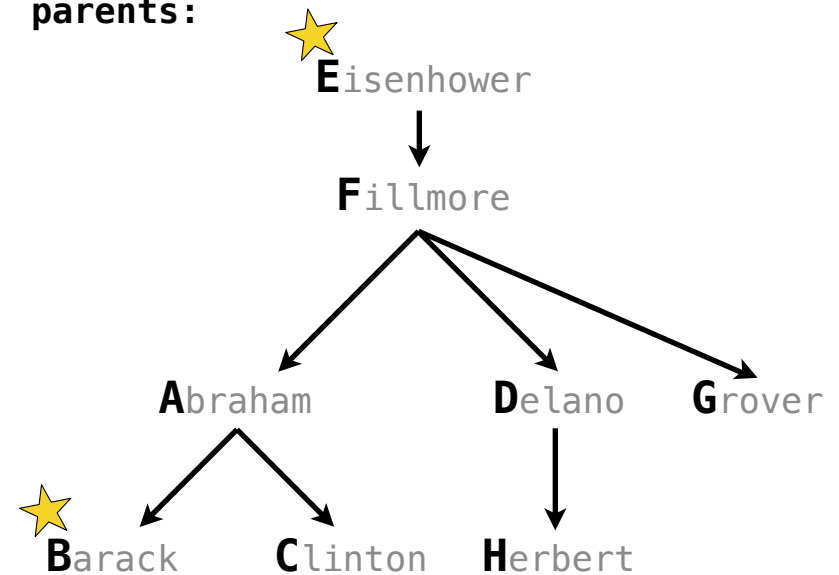
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parents:



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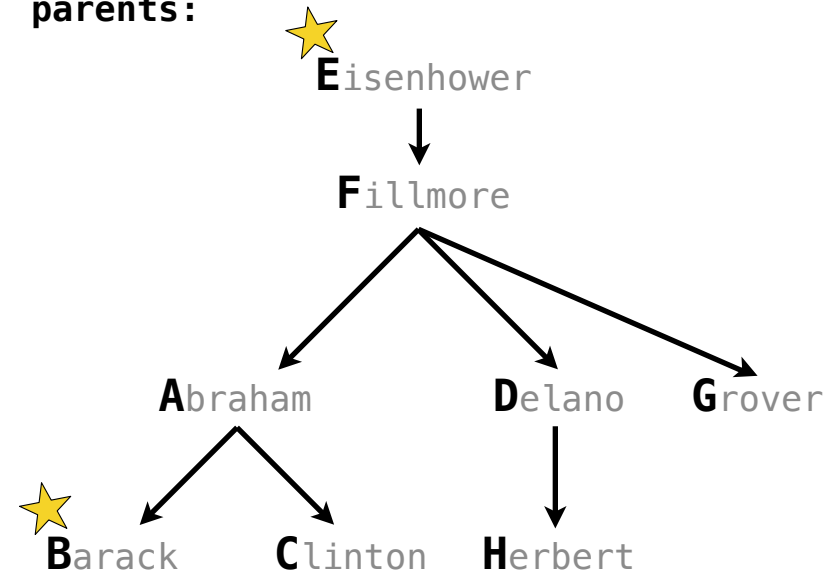
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parents:



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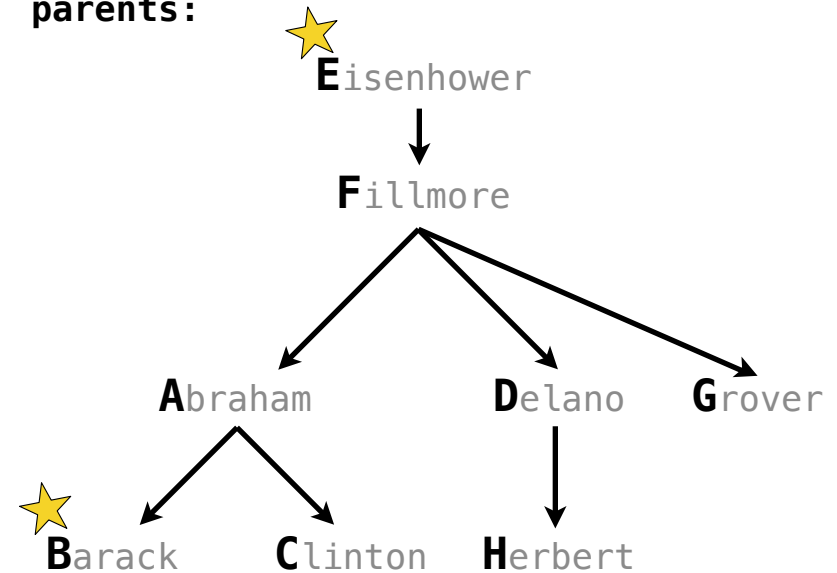
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```
select parent from ...
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parents:



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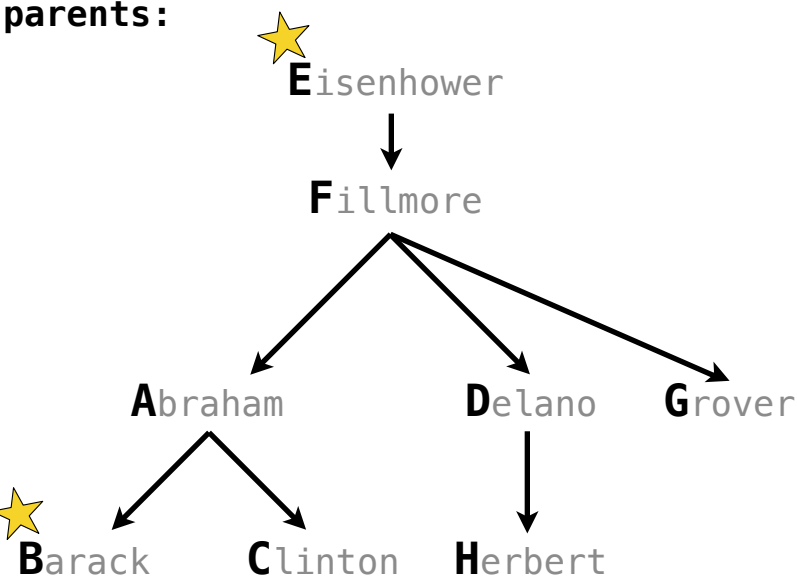
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```
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    select "eisenhower" union
    select "barack"
  )
select parent from ...
```

best:

dog
eisenhower
barack



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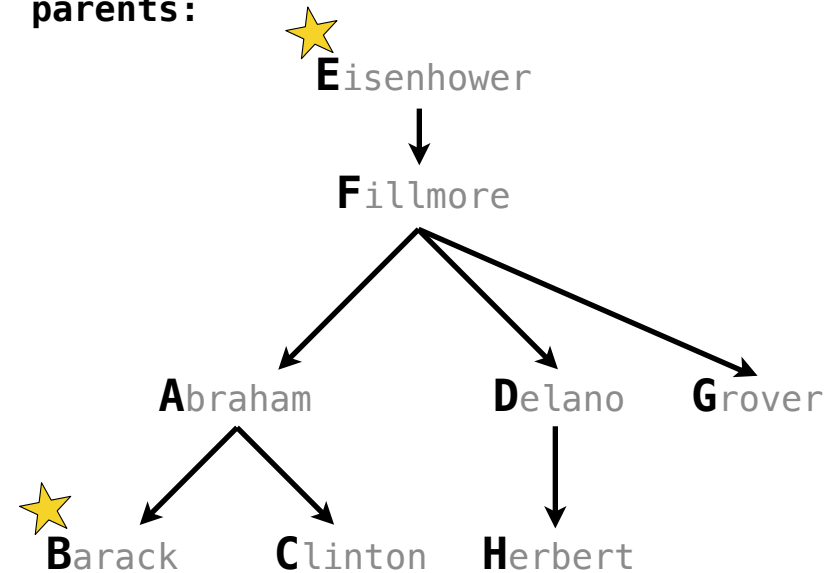
```
best(dog) as (
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)
```

best:

dog
eisenhower
barack

```
select parent from parents, best where child=dog;
```

parents:



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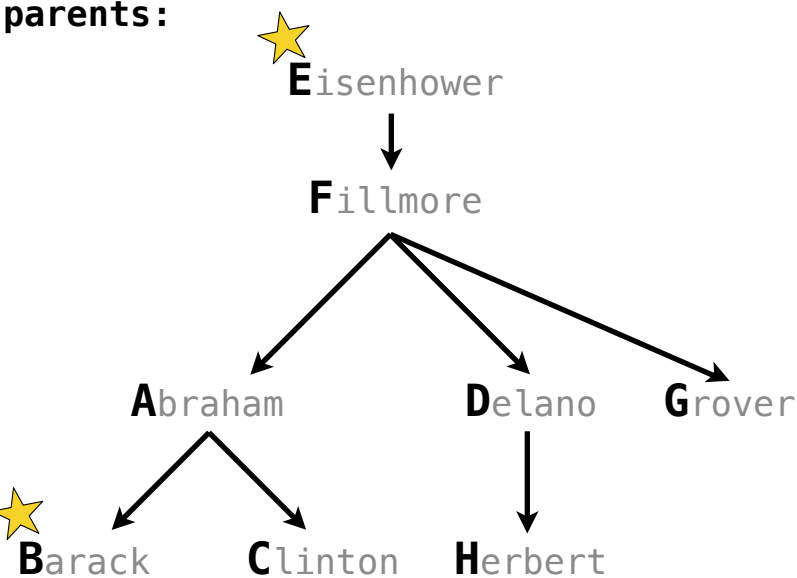
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best(dog) as (
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)
```

best:

dog
eisenhower
barack

```
select parent from parents, best where child=dog;
```

parent
abraham



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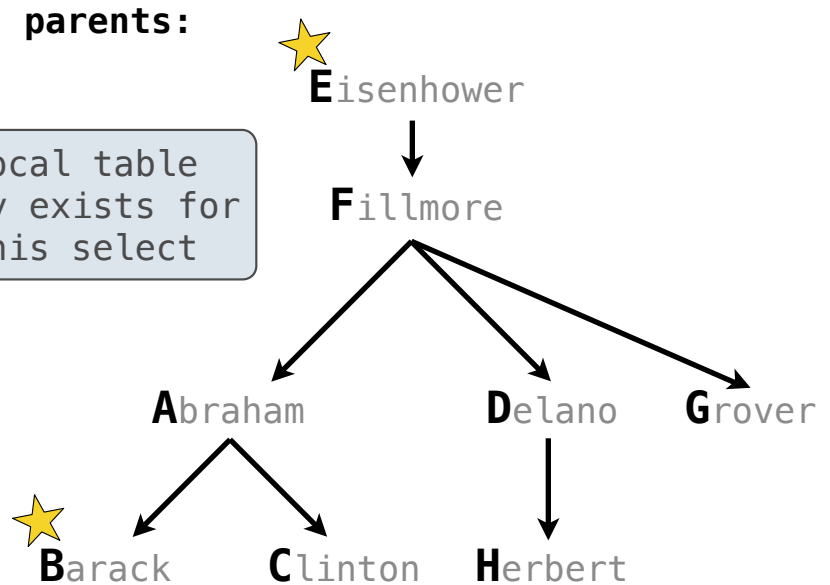
```
  best(dog) as (
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select parent from parents, best where child=dog;
```

parent
abraham

best:
dog
eisenhower
barack

Local table only exists for this select



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```

```
  ...
```

```
with
```

Part of the
select statement

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  best(dog) as (  
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  )
```

```
select parent from parents, best where child=dog;
```

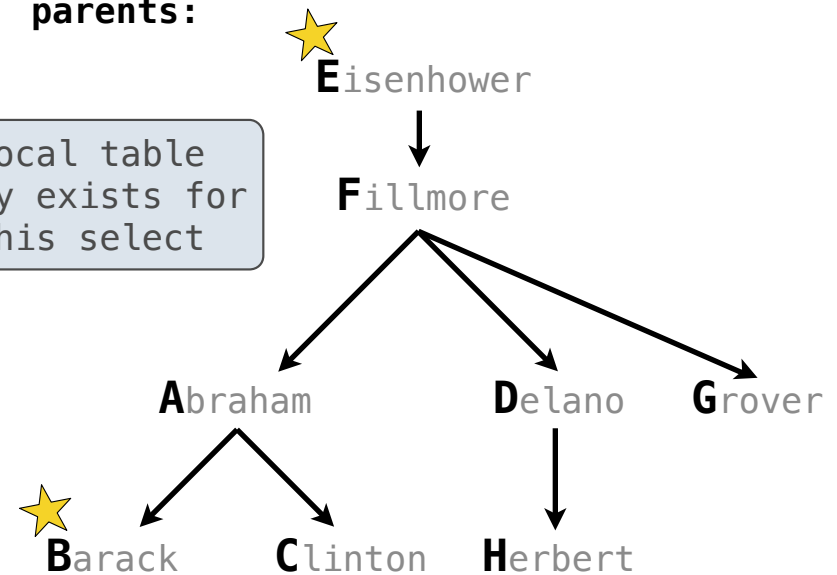
parent
abraham

parents:

best:

dog
eisenhower
barack

Local table
only exists for
this select



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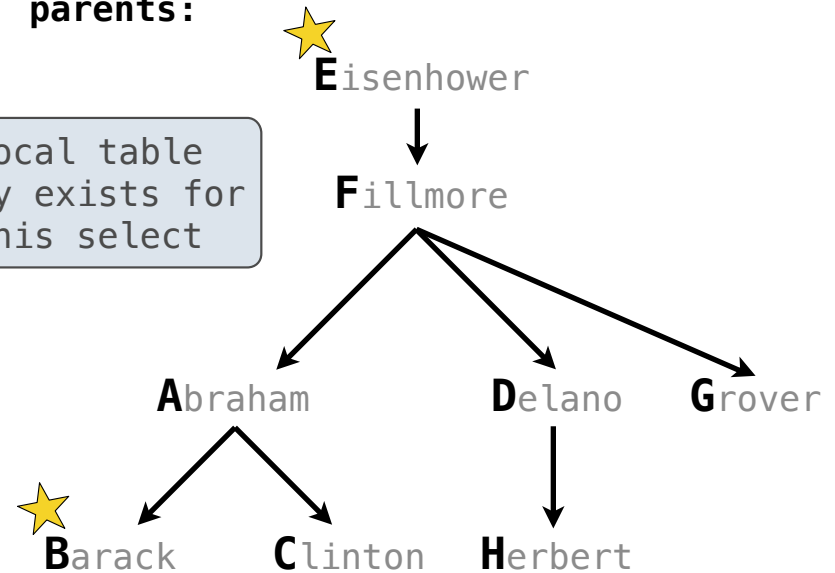
```
select parent from parents, best where child=dog;
```

parent
abraham

(Demo)

parents:

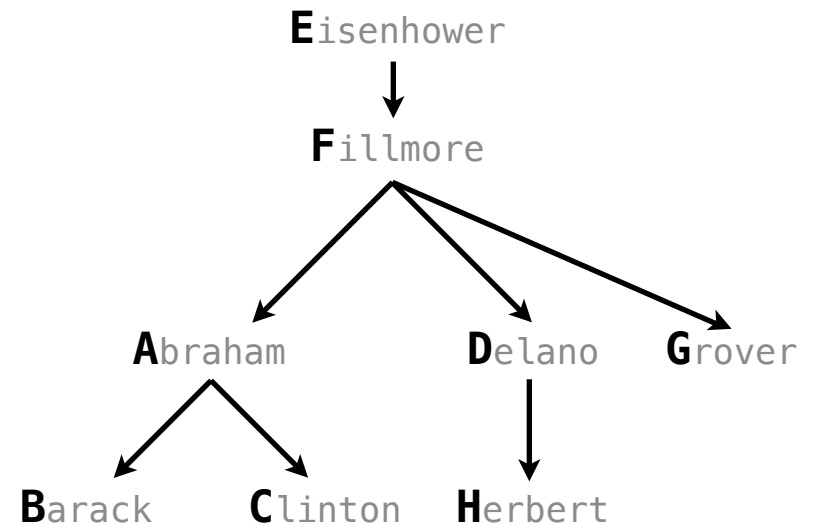
Local table
only exists for
this select



Example: Relationships

```
with
  what(first, second) as (
    select a.child, b.child
           from parents as a, parents as b
           where a.parent = b.parent and
                 a.child != b.child
  )
select child as _____, second as _____
       from parents, what where parent=first;
```

parents:

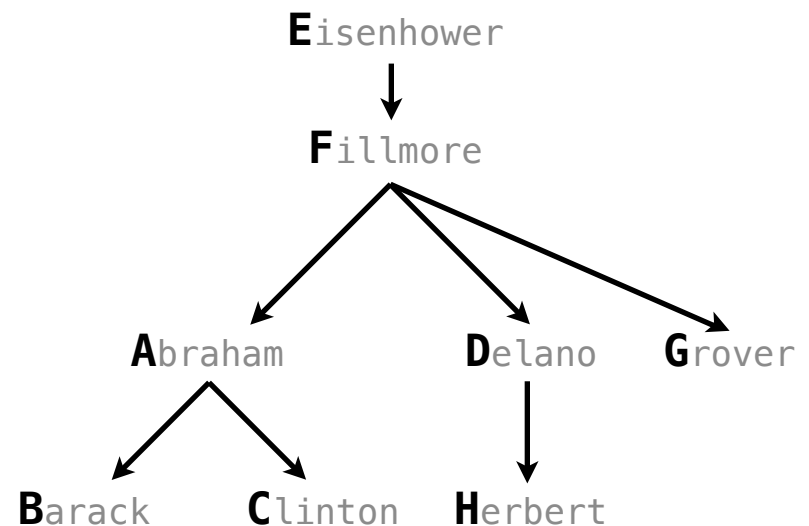


Example: Relationships

(A) What are appropriate names for the columns in this result?

```
with
  what(first, second) as (
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parents:



Example: Relationships

(A) What are appropriate names for the columns in this result?

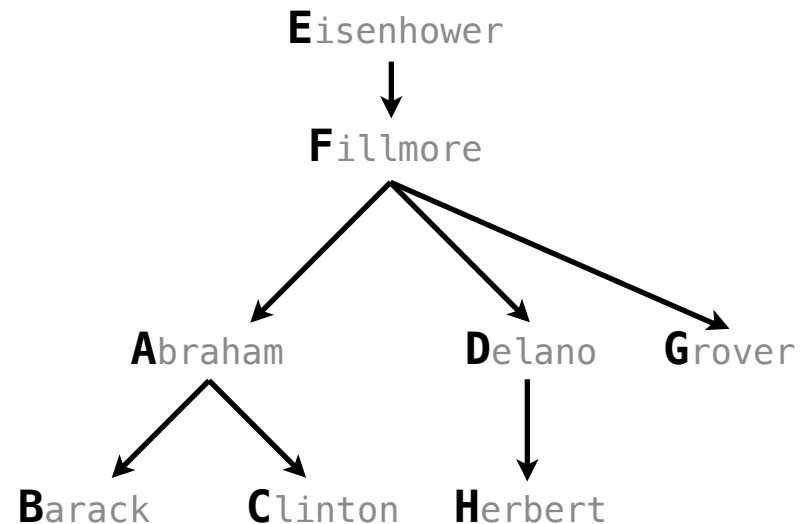
(B) How many rows will result?

with

```
what(first, second) as (  
  select a.child, b.child  
    from parents as a, parents as b  
   where a.parent = b.parent and  
         a.child != b.child  
)
```

```
select child as _____, second as _____  
  from parents, what where parent=first;
```

parents:



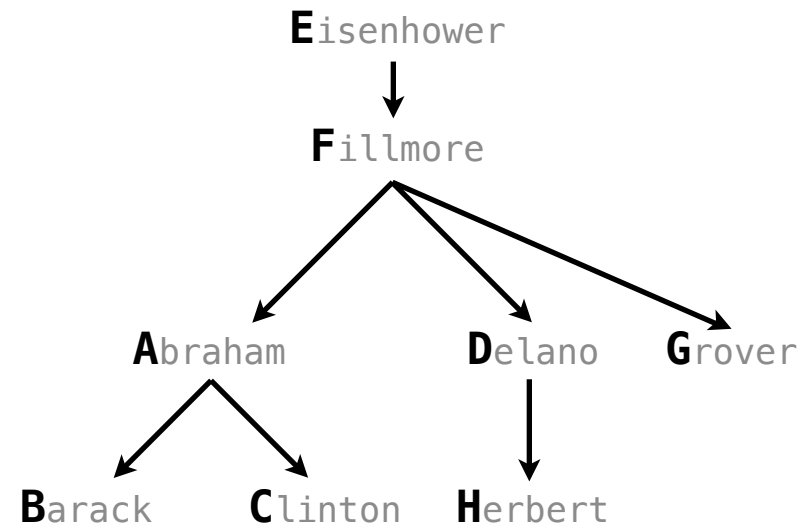
Example: Relationships

(A) What are appropriate names for the columns in this result?

(B) How many rows will result?

```
with
siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as _____, second as _____
       from parents, what siblings
       where parent=first;
```

parents:



Example: Relationships

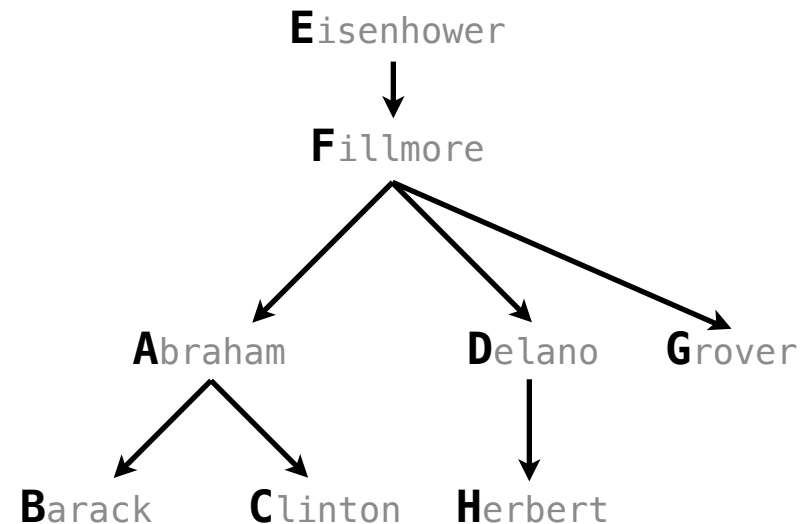
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       from parents, what siblings where parent=first;
```

parent	child	first	second
abraham	barack	abraham	delano

parents:



Example: Relationships

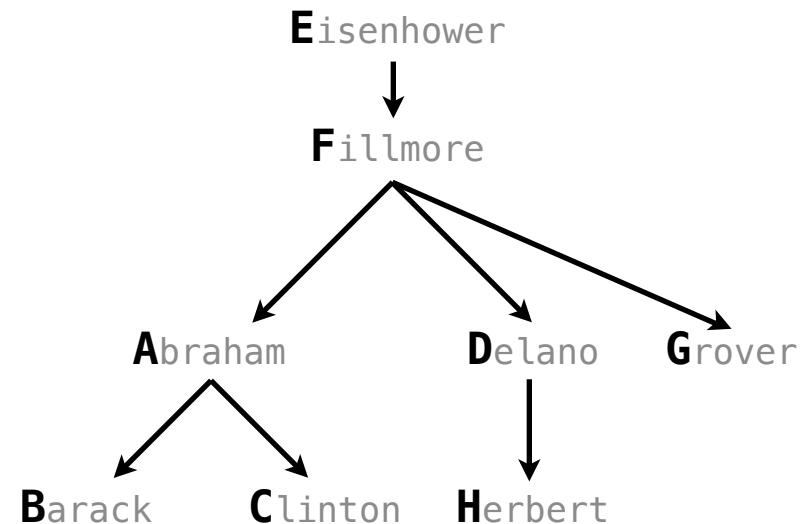
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select child as _____, second as _____
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       where parent=first;
```

parent	child	first	second
abraham	barack	abraham	delano

parents:



Example: Relationships

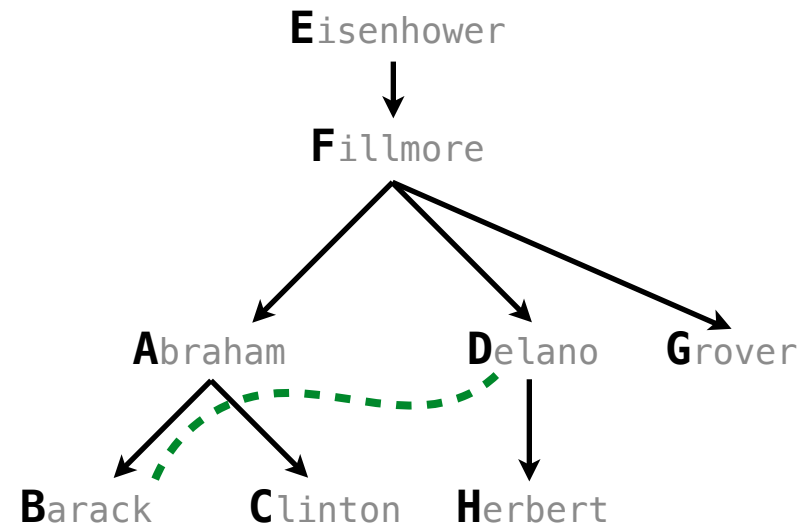
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parents:



Example: Relationships

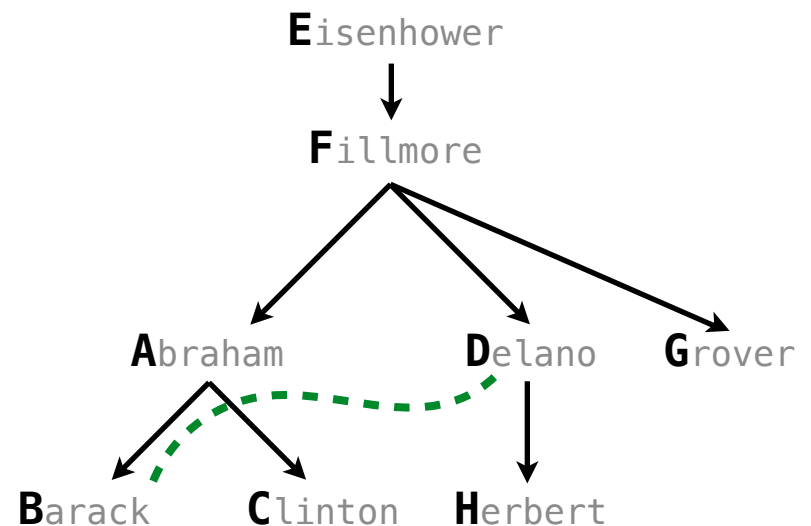
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select child as       , second as       
           from parents, what where parent=first;
                      
```

parent	child	first	second
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parents:



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(A) What are appropriate names for the columns in this result?

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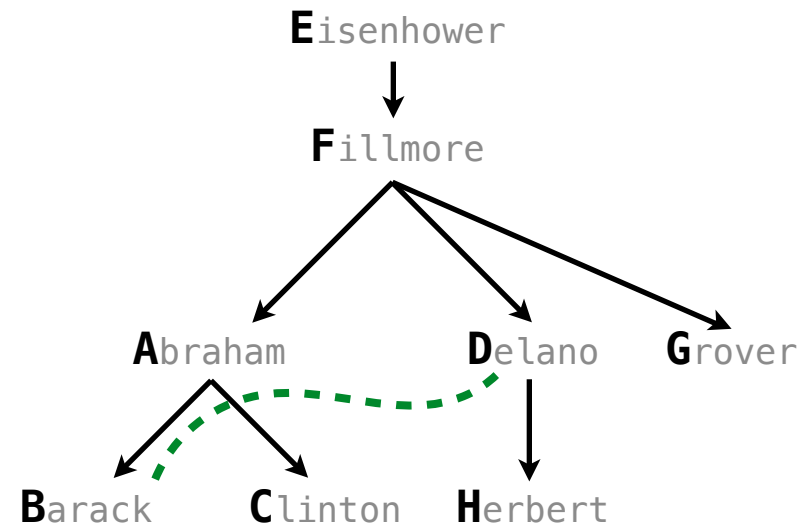
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siblings
what(first, second) as (
  select a.child, b.child
        from parents as a, parents as b
        where a.parent = b.parent and
              a.child != b.child
)
select child as           nephew          , second as           uncle          
        from parents, what           siblings           where parent=first;

```

parent	child	first	second
abraham	barack	abraham	delano

parents:



Recursive Local Tables

Local Tables can be Declared Recursively

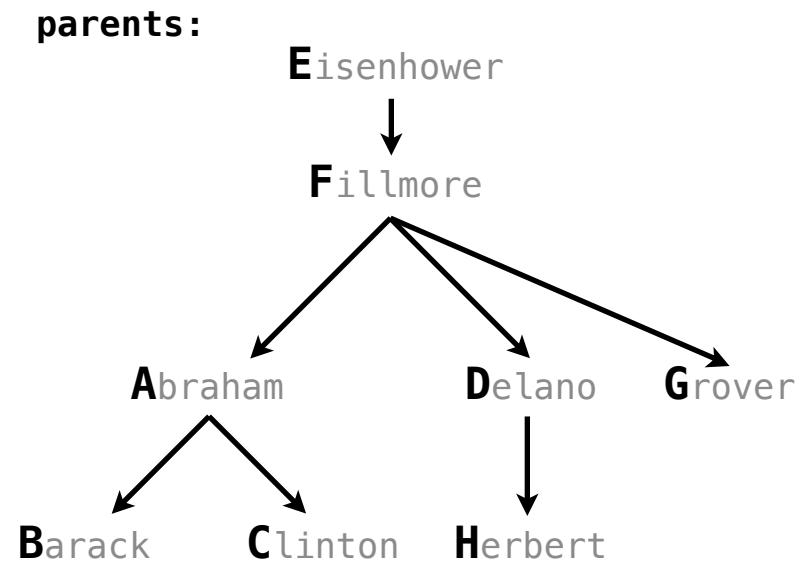
Local Tables can be Declared Recursively

An ancestor is your parent or an ancestor of your parent

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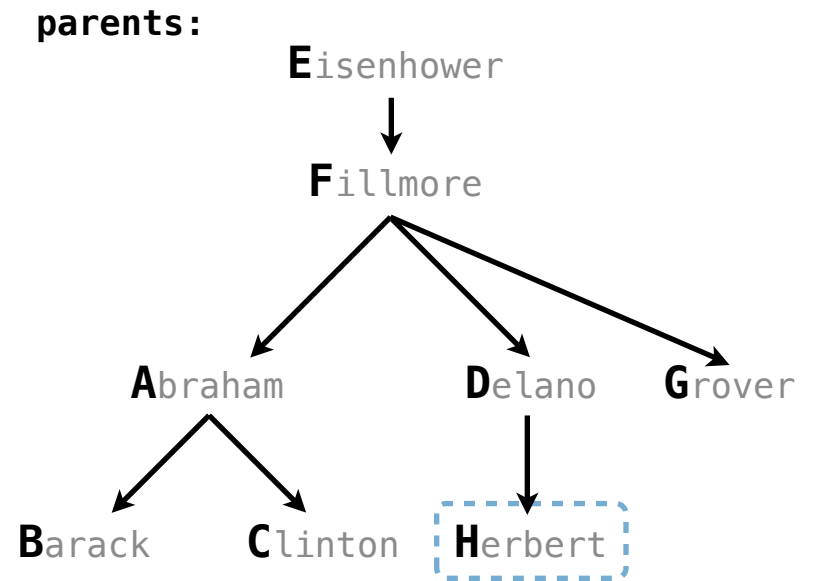
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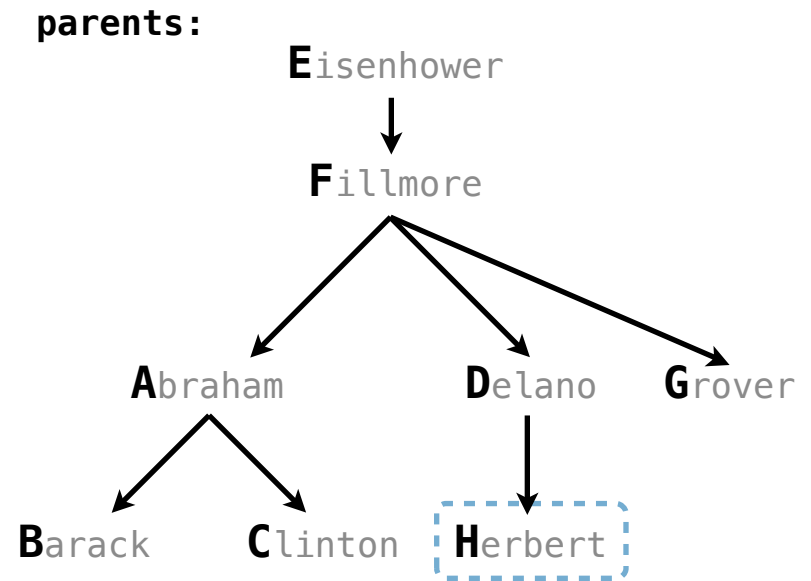


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An ancestor is your parent or an ancestor of your parent

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...
```

ancestors(ancestor, descendent)

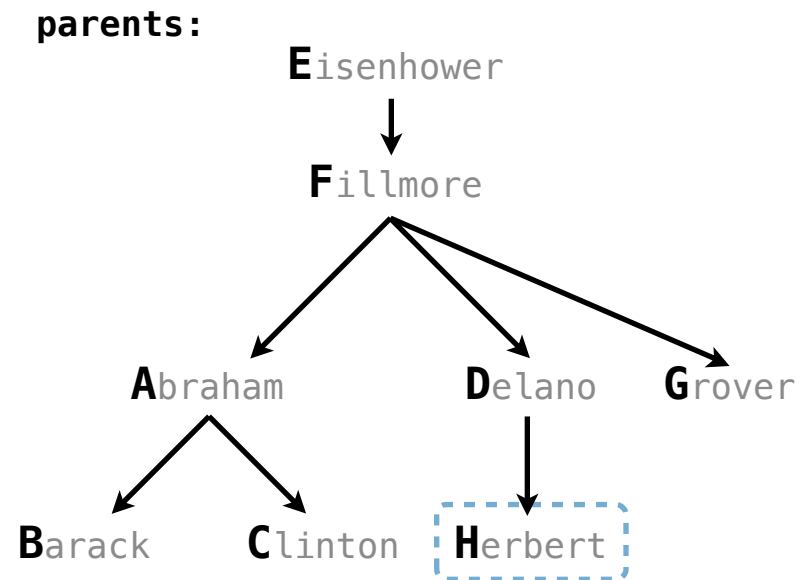


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```

```
ancestors(ancestor, descendent) as (
  select parent, child from parents union
  select ancestor, child
  from ancestors, parents
  where parent = descendent
)
```



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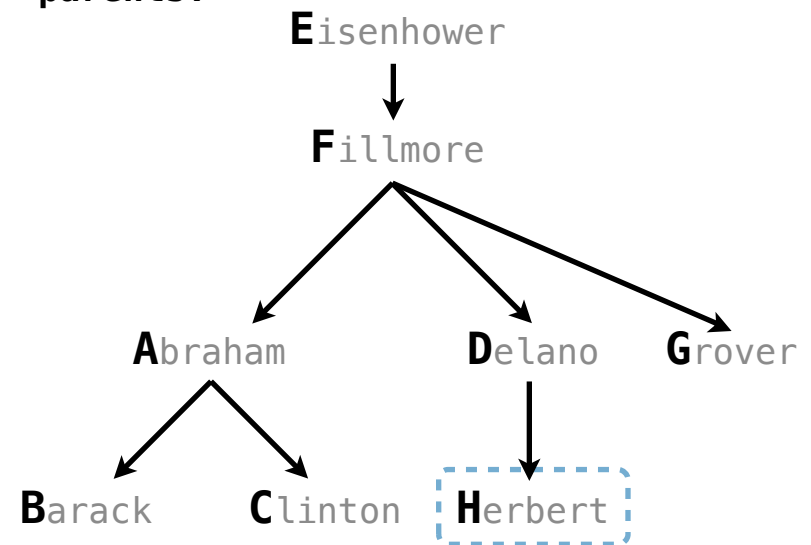
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ancestors(ancestor, descendent) as (
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  select ancestor, child
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  where parent = descendent
```

)

```
select ancestor from ancestors where descendent="herbert";
```

parents:



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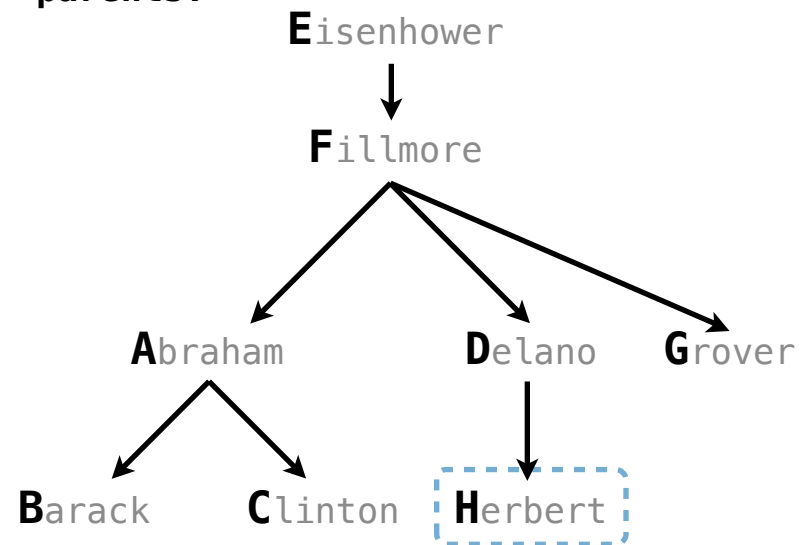
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ancestors(ancestor, descendent) as (
  select parent, child from parents union
  select ancestor, child
  from ancestors, parents
  where parent = descendent
```

)

```
select ancestor from ancestors where descendent="herbert";
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parents:



ancestor
delano
fillmore
eisenhower

Global Names for Recursive Tables

To create a table with a global name, you need to select the contents of the local table

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```
create table odds as
with
  odds(n) as (
    select 1 union
    select n+2 from odds where n < 15
  )
select n from odds;
```

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```

odds:

n
1
3
5
7
9
11
13
15

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Which names above can change without affecting the result?

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odds:

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Which names above can change without affecting the result?

Limits on Recursive Select Statements

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Recursive table definitions are only possible within a with clause

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No mutual recursion: two or more tables cannot be defined in terms of each other

Limits on Recursive Select Statements

Recursive table definitions are only possible within a with clause

No mutual recursion: two or more tables cannot be defined in terms of each other

```
with
  odds(x) as (
    select 1 union select x+1 from evens
  ),
  evens(x) as (
    select x+1 from odds
  )
select x from odds
```

Limits on Recursive Select Statements

Recursive table definitions are only possible within a with clause

No mutual recursion: two or more tables cannot be defined in terms of each other

Nope!

```
with
  odds(x) as (
    select 1 union select x+1 from evens
  ),
  evens(x) as (
    select x+1 from odds
  )
select x from odds
```

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    select x-1 from ints union
    select x+1 from ints
  )
select x from ints;
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```
with
  ints(x) as (
    select 1 union
    select a.x + b.x
      from ints as a, ints as b
  )
select x from ints;
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String Examples

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Noun phrases can contain relative pronouns that introduce relative clauses


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(Demo)

Integer Examples

Input-Output Tables

A table containing the inputs to a function can be used to map from output to input

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```
create table pairs as
with
  i(n) as (
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    select n+1 from i where n < 50
  )
select a.n as x, b.n as y from i as a, i as b where a.n <= b.n;
```

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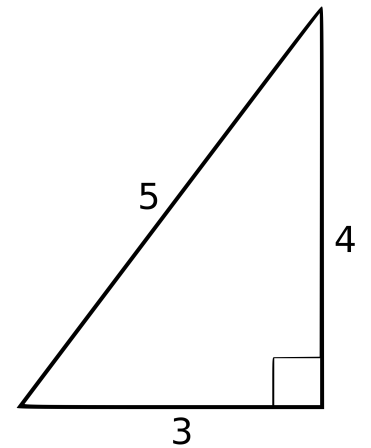
(Demo)

Example: Pythagorean Triples

All triples a, b, c such that $a^2 + b^2 = c^2$

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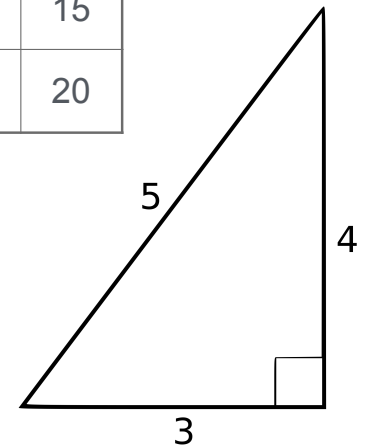
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Example: Pythagorean Triples

All triples a , b , c such that $a^2 + b^2 = c^2$

a	b	c
3	4	5
5	12	13
6	8	10
8	15	17
9	12	15
12	16	20



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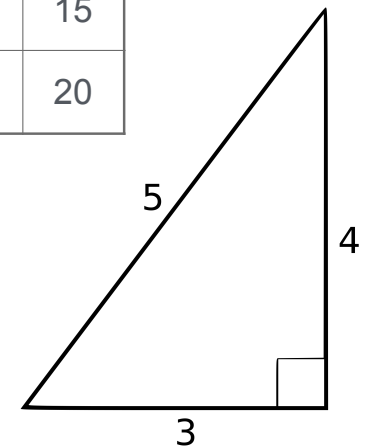
`)`

`select a.n as a, b.n as b, c.n as c`

`from _____`

`where _____ and a.n*a.n + b.n*b.n = c.n*c.n;`

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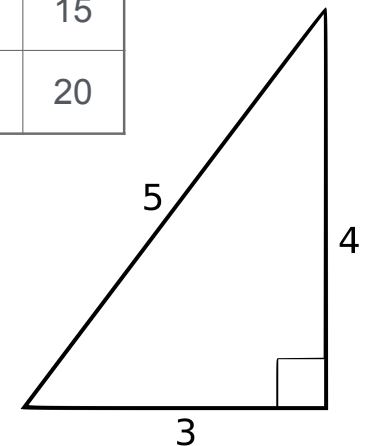
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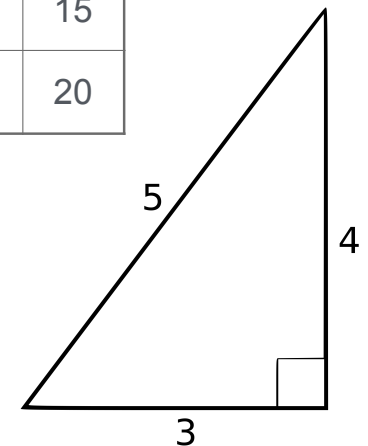
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`select a.n as a, b.n as b, c.n as c`

`from _____`
`i as a, i as b, i as c`

`where _____`
`a.n < b.n` and `a.n*a.n + b.n*b.n = c.n*c.n;`

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Example: Fibonacci Sequence

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Computing the next Fibonacci number requires both the previous and current numbers

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fib:

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Computing the next Fibonacci number requires both the previous and current numbers

```
create table fibs as
with
  fib(previous, current) as (
    select 0, 1 union
    select current, previous+current from fib
    where current <= _____
  )
select _____ as n from fib;
```

fibs:

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```

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n
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A Very Interesting Number

The mathematician G. H. Hardy once remarked to the mathematician Srinivasa Ramanujan...

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